

Chaos, bifurcations and strange attractors in environmental radioactivity dynamics of some geosystems

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Abstract: We develop the theoretical foundations of new universal complex chaos-dynamical approach to description of the deterministic chaos, bifurcations and strange attractors in dynamics of the environmental radioactivity systems. In particular, the atmospheric radon ^{222}Rn concentration temporal dynamics is studied and computed. The nonlinear analysis methods include advanced versions of the correlation integral and multifractal analysis, algorithms of average mutual information, false nearest neighbors, surrogate data, Lyapunov's exponents and Kolmogorov's energy analysis, non-linear prediction schemes, predicted trajectories algorithms, spectral methods etc (in versions [1,2]). The chaos-dynamical approach is applied to quantitative analysis, modeling and forecasting temporal and spatial evolution of the atmospheric radon ^{222}Rn concentration. The detailed data of measurements of the radon concentrations at Environmental Measurements Laboratory (US Department of Energy, and Goddard Institute of Space Studies Chester, New Jersey, USA (1978-2001; c.g.[3]) are used. The perspectives of computing chaos, bifurcations and strange attractors characteristics in other geo- and bio-systems are analyzed. References: [1] Glushkov A.V.: Methods of a Chaos Theory. Odessa: Astroprint, 2012. [2] Glushkov A.V., Khetselius O.Yu., Svinarenko A.A., Buyadzhi V.V.: Methods of computational mathematics and mathematical physics, P.1. Odessa: TEC, 2015. [3] Jacob D., Prather M.: Tellus. 42b, 118 (1990).

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